# Analysis of Biological Networks and Related Data 

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## Analysis of Biological Networks

(1) Motivation
(2) Foundations
(3) Network motifs
(9) Network centralities
(6) Network-related data analysis and visualisation

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## From Biological Building Blocks to Complex Systems

## From Biological Building Blocks to Complex Systems



Genes Transkripts Proteins Metabolites

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Genes
Transkripts Proteins
Metabolites

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Genes
Transkripts
Proteins
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## From Biological Building Blocks to Complex Systems



## From Biological Building Blocks to Complex Systems



## Embedding in Space and Time



## Embedding in Space and Time

$\xrightarrow[\text { reactions development }]{ } \quad \underset{\text { evolution }}{\text { time }}$
dynamic structure
compartments tissues organs
environment

## Embedding in Space and Time



## Embedding in Space and Time

Integrative Bioinformatics Systems Biology Network analysis

## Bioinformatics Research Areas

Representation


Visualisation
Analysis

## Bioinformatics Research Areas



Visualisation
Analysis

## Bioinformatics Research Areas

Data structures
Databases \& information systems
Data integration
Representation


Visualisation
Analysis

> | Algorithms |
| :---: |
| Simulation |
| Theoretical CS |
|  |
| machine learning |

## Bioinformatics Research Areas

Data structures
Databases \& information systems
Data integration
Representation


Visualisation
Visualisation \& computer graphics Human-computerinteraction

Analysis

> Algorithms Simulation
> Theoretical CS Statistics \& machine learning

## Biological Networks

- Metabolic pathways
- Protein interaction networks
- Gene regulatory networks
- Signal transduction pathways
- Hormonal networks
- Food webs
- Evolutionary networks


Protein Interactions of Mus musculus Source: DIP (Database of Interacting Proteins)

## Biological Networks

- Networks get more complex
- Methods for the analysis of networks are required
- Several methods focus on structural analysis of networks


Protein Interactions of Saccharomyces cerevisiae
Source: DIP (Database of Interacting Proteins)

## Example 1: Centralities in Biological Networks

Phenotypic effect of protein removal in S. cerevisiae: likelihood of lethal effects positively correlates with number of interactions

## Effects:

- lethal (red)
- non-lethal (green)
- slow growth (orange)
- yellow (unknown)


Paiek
Lethality and centrality in protein networks [Jeong et al., 2001]

## Example 2: Network Alignment and Comparison

Applications for comparative analysis:

- Development of speciesspecific drug targets
- Identification of previously unknown parts of network in a species
- Understanding evolutional relationships between species


Visual comparison of metabolic pathways (BioPath)

## Example 3: Network-related Data Analysis

| Measurements |  |  |  | Substance | L-Rhamnose | D-Glucose | D-Fructose | Sucrose | Kestose |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plant/ |  |  |  | Meas.Tool | IC | IC | IC | 1 C | IC |
| Genotype | Replicate \# | Time | Unit (Time) | Unit | $\mu \mathrm{mol} / \mathrm{g}$ FW | $\mu \mathrm{mol} / \mathrm{g} \mathrm{FW}$ | jmol / g FW | $\mu \mathrm{mol} / \mathrm{g} \mathrm{FW}$ | $\mu \mathrm{mol} / \mathrm{g} \mathrm{FW}$ |
| 1 | 1 | 0 | day |  | 1.727672479 | 21.52691433 | 22.68415466 | 23.4884003 | 5.33484579 |
| 1 | 2 | 0 | day |  | 2.286812227 | 20.60995633 | 24.55126638 | 29.5486463 | 6.65596611 |
| 1 | 3 | 0 | day |  | 1.932139879 | 20.18324777 | 23.63030326 | 28.4753847 | 5.98485434 |
| 1 | 1 | 2 | day |  | 1.577154725 | 17.45711319 | 19.24278297 | 31.4654206 | 9.26147767 |
| 1 | 2 | 2 | day |  | 1.826811181 | 17.27461495 | 21.96098118 | 35.9760411 | 10.0532132 |
| 1 | 3 | 2 | day |  | 1.634978998 | 17.31494548 | 20.95633188 | 33.4853284 | 9.5943838 |
| 1 | 1 | 4 | day |  | 1.865477252 | 25.74130241 | 37.22247993 | 42.4235504 | 8.8479397 |
| 1 | 2 | 4 | day |  | 2.21747397 | 19.40461747 | 29.68076053 | 38.96134 | 8.91434024 |
| 1 | 3 | 4 | day |  | 2.02328452 | 22.04847397 | 35.21072447 | 39.4956783 | 8.73244834 |
| 1 |  | 6 | day |  | 1.920580762 | 19.44508167 | 20.3522323 | 77.1737205 | 11.8247024 |
| 1 | 2 | 6 | day |  | 1.998378179 | 20.11116845 | 20.56852193 | 69.4410616 | 11.7584525 |
| 1 | 3 | 6 | day |  | 1.962938283 | 19.24282989 | 20.45439912 | 74.495839 | 11.7234494 |
| 1 | 1 | 8 | day |  | 1.458018305 | 20.00477517 | 12.57461202 | 68.0601671 | 10.7323839 |
| 1 | 2 | 8 | day |  | 1.482652134 | 16.16039964 | 6.447048138 | 66.3048953 | 10.4583938 |
| 1 | 3 | 8 | day |  | 1.469294299 | 17.21457188 | 9.552893255 |  |  |
| 1 | 1 | 10 | day |  | 0.765296389 | 9.776606859 | 10.22575517 | 69.3750625 | 8.47657779 |
| 1 |  | 10 | day |  | 0.805443411 | 9.242549331 | 10.45243819 | 62.0314811 | 8.4270846 |
| 1 | 3 | 10 | day |  | 0.791929124 | 9.267393562 | 10.34295904 | 65.3948543 | 8.4539934 |
| 1 | 1 | 12 | day |  | 0.503449651 | 3.582851446 | 7.037128614 | 40.9261815 | 6.57479561 |
| 1 | 2 | 12 | day |  | 0.602908184 | 4.254590777 | 7.41354383 | 40.8603241 | 6.22086315 |
| 1 | 3 | 12 | day |  | 0.554383723 | 3.875642656 | 7.204345494 | 40.8238434 | 6.43549495 |
| 1 | 1 | 14 | day |  | 0.328968441 | 1.897032501 | 8.911257654 | 46.8580311 | 9.85379821 |
| 1 | 2 | 14 | day |  | 0.312160058 | 2.479645382 | 9.529555529 | 44.5088295 | 10.6903733 |
| 1 | 3 | 14 | day |  | 0.313432342 | 2.243456446 | 9.345948533 | 46.0034853 | 10.3404599 |
| 1 | 1 | 15 | day |  | 0.281327014 | 2.2307109 | 9.55563981 | 42.0390521 | 10.1148568 |
| 1 | 2 | 16 | day |  | 0.252511307 | 2.072363723 | 9.97314925 | 36.8065699 | 10.65319 |
| 1 | 3 | 16 | day |  |  |  |  |  |  |
| 1 | 1 | 18 | day |  | 0.180939078 | 1.6511443 | 4.144923176 | 32.2245192 | 10.1636649 |
| 1 | 2 | 18 | day |  | 0.172426673 | 1.69816544 | 4.469471603 | 32.602263 | 10.6836445 |
| 1 | 1 | 20 | day |  | 0.141456852 | 2.085412262 | 4.131462618 | 37.623448 | 11.5464876 |
| 1 | 2 | 20 | day |  | 0.229693448 | 2.334441996 | 2.508595472 | 40.7439792 | 11.4419987 |

## Example 3: Data Analysis without the Network Context



## Example 3: Data Analysis within the Network Context



Clustering based on self-organising map (SOM)

## Example 3: Data Analysis within the Network Context



Three phases in seed development
(pre-storage, intermediate and main storage)

## Analysis of Biological Networks

(1) Motivation
(2) Foundations
(3) Network motifs
(9) Network centralities
(6) Network-related data analysis and visualisation

## Graphs and Networks

- Network is an informal description for a set of elements with connections or interactions between them and data attached to them
- Graph is a formal description, it is a mathematical object consisting of vertices and edges representing elements and connections, respectively


## Graphs

- Graph: $G=(V, E)$
- Set of vertices: $V(n=|V|)$
- Set of edges: $E \subseteq V \times V(m=|E|)$
- Neighbourhood of a vertex: $N(u)=\{v:(u, v) \in E\}$
- Adjacency matrix for $G:(n \times n)$ matrix, where $a_{i j}=1$ if and only if $(i, j) \in E$ and $a_{i j}=0$ otherwise


$$
A=\left(\begin{array}{llllll} 
& a & b & c & d & e \\
a & 0 & 1 & 0 & 0 & 1 \\
b & 1 & 0 & 0 & 0 & 1 \\
c & 0 & 0 & 0 & 1 & 1 \\
d & 0 & 0 & 1 & 0 & 0 \\
e & 1 & 1 & 1 & 0 & 0
\end{array}\right)
$$

## Graphs

- Degree of a vertex: number of its incident edges $(d(v))$
- Walk: sequence of edges connecting vertices $\left(e_{1}, \ldots, e_{k}\right)$
- Length of a walk: number of edges, $k=\left|\left(e_{1}, \ldots, e_{k}\right)\right|$
- Path: walk where edges are pairwise distinct
- Shortest path: a minimal length path between $u$ and $v$

$d(a)=2$
Walk:
$((a, b),(b, a),(a, b),(b, e),(e, c))$
Path: $((a, b),(b, e),(e, c))$
Shortest path: $((a, e),(e, c))$


## Graphs

- Distance: length of a shortest path between two vertices (dis t(u,v))
- Connected graph: a walk exists between every two vertices
- Random walk: starting at vertex $u$ chooses uniformly at random an incident edge until reaching $v$
- Subgraph: of $G=(V, E)$ is a graph $G^{\prime}=\left(V^{\prime}, E^{\prime}\right)$, where $V^{\prime} \subseteq V$, and $E^{\prime} \subseteq E \cap V^{\prime} \times V^{\prime}$

Consider non-trivial, loop-free, connected graphs
 $\operatorname{dist}(a, c)=2$
Random walk from $a$ to $c$ :
$((a, e),(e, a),(a, b),(b, e),(e, c))$ Subgraph: $V^{\prime}=\{a, b, e\}$ and

$$
E^{\prime}=\{(a, b),(a, e)\}
$$

## Graphs - Types

- Undirected graphs
- Directed graphs
- Mixed graphs
- Labelled graphs (vertices, edges)
- Multi-graphs


## Graphs - Types

- Hyper-graphs
consists of a set of vertices and a set of hyper-edges, each hyper-edge is a non-empty subsets of the node set $V$
- Bipartite graphs vertex set $V$ can be partitioned in two disjoint, nonempty sets $V_{1}$ and $V_{2}$ such that each edge in $E$ has exactly one end-vertex in $V_{1}$ and one end-vertex in $V_{2}$

vertices of $\mathrm{V}_{1}$


## Graph visualisation

- Graphical representation of a graph
- Draw a point for each vertex and a line for each edge which connects the corresponding points of its end-vertices
- The positions of the vertices and the drawing of the lines is called the layout of the graph



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## Motivation

Motif detection in networks:

- searching
- counting
- visual exploration


Motif size: $\left|E_{p}\right|$


Target graph $G_{t}=\left(V_{t}, E_{t}\right)$ with highlighted motif matches size: $\left|E_{t}\right|$

## Motivation

Interesting motifs are found in biological networks:

- Gene regulatory networks
- Metabolic networks
- Protein-protein interaction networks
- Neuronal networks, food-webs


## Network Motifs

- Particular subgraphs representing patterns of local interconnections between network elements
- May represent basic building blocks and design patterns of functional modules
- Overabundance may be a consequence of positive selection due to functional or structural properties

[Babu et al., 2004]


## Motifs in Gene Regulatory Networks: Feed-forward Loop

Functional properties of the feed-forward loop motif in gene regulation

- Noise filtering: responds only to persistent activations


Network motifs in the transcriptional regulation network of Escherichia coli [Shen-Orr et al., 2002]

## Analysing Networks and Finding Interesting Motifs

Frequent motifs in networks

- Motif frequency: number of matches in the target graph
- Motifs with high frequency are potential candidates for functional network motifs
- Different concepts for frequency determination as a result of different restrictions of the reuse of graph elements
$\rightarrow$ Motif Frequency Concepts


## Concepts for Determination of Motif Frequency

| Concept | Graph element reuse |  | Frequency determination |
| :---: | :---: | :---: | :--- |
|  | Vertices | Edges |  |
| $\mathcal{F}_{1}$ | yes | yes | All matches |



## Concepts for Determination of Motif Frequency

| Concept | Graph element reuse |  | Frequency determination |
| :---: | :---: | :---: | :--- |
|  | Vertices | Edges |  |
| $\mathcal{F}_{1}$ | yes | yes | All matches |
| $\mathcal{F}_{2}$ | yes | no | Maximum independent set |



## Concepts for Determination of Motif Frequency

| Concept | Graph element reuse |  | Frequency determination |
| :---: | :---: | :---: | :--- |
|  | Vertices | Edges |  |
| $\mathcal{F}_{1}$ | yes | yes | All matches |
| $\mathcal{F}_{2}$ | yes | no | Maximum independent set |
| - | no | yes | - |



## Concepts for Determination of Motif Frequency

| Concept | Graph element reuse |  | Frequency determination |
| :---: | :---: | :---: | :--- |
|  | Vertices | Edges |  |
| $\mathcal{F}_{1}$ | yes | yes | All matches |
| $\mathcal{F}_{2}$ | yes | no | Maximum independent set |
| - | no | yes | - |
| $\mathcal{F}_{3}$ | no | no | Maximum independent set |


$\mathcal{F}_{1}$ Does not exclude matches

- Shows the full potential of the motif
$\mathcal{F}_{2}$ - Matches does not share relation of elements
- Shows the maximum number of instances of a particular motif which can be active at the same time
$\mathcal{F}_{3}$
- Matches can be seen as non-overlapping clusters
- Allows specific analysis and navigation methods
- Folding and unfolding of clusters
- Motif preserving layout of the matches


## Frequent Motif Search - Problems

- Many different motifs:

| Rev. edges | - | + | - | + |
| :---: | ---: | ---: | ---: | ---: |
| Self loops | - | - | + | + |
| Motif size |  |  |  |  |
| 2 | 3 | 4 | 5 | 6 |
| 3 | 10 | 12 | 18 | 21 |
| 4 | 39 | 53 | 76 | 97 |
| 5 | 169 | 237 | 361 | 478 |
| 6 | 876 | 1306 | 1978 | 2762 |
| 7 | 4834 | 7537 | 11658 | 17002 |
| 8 | 29316 | 47913 | 74494 | 113528 |
| 9 | 189054 | 322253 | 505277 | 801966 |

- Many different matches for one motif: $O\left(\left|E_{t}\right|^{\left|E_{p}\right|}\right)$

There is an giant number of possible motif matches!

- Search motifs of given size with maximum frequency:
- Given: graph $G=(V, E)$, target size $t$, frequency concept $\mathcal{F}$
- Result: Motif with maximum frequency (and frequency)
- Several extensions:
- Application of different frequency concepts
- Full control over the search, e.g. define frequency threshold
- Parallel implementation of the search algorithm
- Idea:
- Start of search with the motif of size 1
$\rightarrow$ each edge of target graph used to create a match
- While (motifs for extension are left)
$\rightarrow$ extend next motif by addition of one edge (combine match with each incident edge to new motif)
$\rightarrow$ compute frequency for each new motif and if frequency is above threshold than keep motif (adjust threshold)


## Traversal of the Space of all Motifs

- Each motif is assigned to parent motif of size $n-1$
- Only generation of the motifs supported by the target graph
- Depth first traversal of the motif tree
- Allows pruning of infrequent branches for $\mathcal{F}_{2}$ and $\mathcal{F}_{3}$



## Problem

- Many different motifs

| Rev. edges <br> Self loops | - | + | $\ldots$ |
| :---: | ---: | ---: | :--- |
| Motif size | - | - | $\ldots$ |
| 2 |  |  |  |
| 3 | 3 | 4 | $\ldots$ |
| 4 | 10 | 12 | $\ldots$ |
| 5 | 39 | 53 | $\cdots$ |
| 6 | 169 | 237 | $\cdots$ |
| 7 | 876 | 1306 | $\cdots$ |
| 8 | 4834 | 7537 | $\cdots$ |
| 9 | 29316 | 47913 | $\cdots$ |
|  | 189054 | 322253 | $\cdots$ |

## Solution

- Only consider motifs supported by target graph
- Building and pruning of motif tree

- Parallel computation


## Problem

- Many different matches for one motif: $O\left(\left|E_{t}\right| E^{\left|E_{p}\right|}\right)$
- Maximum independent set
- Graph isomorphism


## Solution

- Only extension of matches of parent motif
- Use of heuristic
- Canonical labelling


## Problem

- Many different matches for one motif: $O\left(\left.\left|E_{t}\right|\right|^{\left|E_{p}\right|}\right)$
- Maximum independent set
- Graph isomorphism
- In worst case computational very expensive


## Solution

- Only extension of matches of parent motif
- Use of heuristic
- Canonical labelling
- In practise for moderate sized networks applicable


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## Network Centralities

Ranking of vertices according to importance based on the network structure

Applications of centralities:

- Prioritisation of potential drug targets
- Hypothesis generation for experiments
- Exploration of a network
- Determination which patients should be vaccinated first


Protein Interactions of Mus musculus Source: DIP (Database of Interacting Proteins)

## Informal Definition of Centrality

- Let $G=(V, E)$ be a graph
- A function $\mathcal{C}: V \mapsto \mathbb{R}$ is called a centrality
- We say $u \in V$ is more important than $v \in V$ with respect to a given centrality $\mathcal{C}$ if $\mathcal{C}(u)>\mathcal{C}(v)$
- A centrality allows us to order the vertices
- Convention: "Important" vertices get a high centrality value



## Centralities in Biological Networks

- Ranking of vertices according to importance
- Based on the network structure
- Many different (>20) centrality measures exist
- Examples: Degree-Centrality, Eccentricity-Centrality, Closeness-Centrality, Random Walk Betweenness-Centrality, Eigenvector-Centrality

|  | Degree | Closeness | SPBetw |
| :--- | :--- | :--- | :--- |
| 1 | DIP:320N | DIP:369N | DIP:320N |
| 2 | DIP:24169N | DIP:1048N | DIP:369N |
| 3 | DIP:493N | DIP:320N | DIP:1048N |
| 4 | DIP:24196N | DIP:24196N | DIP:24196N |
| 5 | DIP:442N | DIP:24169N | DIP:24169N |



## Degree-Centrality

- Number of incident edges to $v$
- degree-centrality: $\mathcal{C}_{d}(v):=d(v)$
- Jeong et al. reports the correlation of removal of high degree proteins with lethality for the organism (Jeong et al., 2002)



## Eccentricity-Centrality

- eccentricity ecc of a vertex $u$ is defined as $\operatorname{ecc}(u):=\max _{v \in V} \operatorname{dist}(u, v)$
- eccentricity-centrality: $\mathcal{C}_{e}(u):=\frac{1}{\operatorname{ecc}(u)}$
- Applied by Wuchty et al. to compute the "central" metabolites of the metabolic network (Wuchty et al., 2003)


| $v$ | $\mathcal{C}_{e}(v)$ |
| :---: | :---: |
| $a$ | 0.333 |
| $b$ | 0.333 |
| $c$ | 0.5 |
| $d$ | 0.333 |
| $e$ | 0.5 |

## Closeness-Centrality

- Use sum of distances to all other vertices, i.e. sumdist $(u)=\sum_{v \in V} \operatorname{dist}(u, v)$
- closeness-centrality: $\mathcal{C}_{c}(u):=\frac{1}{\text { sumdist }(u)}$
- Also applied by Wuchty et al. to compute the central metabolites of the metabolic network (Wuchty et al., 2003)


| $v$ | $\mathcal{C}_{c}(v)$ |
| :---: | :---: |
| $a$ | 0.143 |
| $b$ | 0.143 |
| $c$ | 0.167 |
| $d$ | 0.111 |
| $e$ | 0.2 |

## Random Walk Betweenness-Centrality

- Betweenness: Observe communication in the network
- A vertex $u$ can observe the communication between $v$ and $w$ if $u$ lies in the path of the communication
- Different methods to model communication
- random-walk betweenness centrality $\mathcal{C}_{r}(u)$ is equal to the number of times a random walk from $v$ to $w$ goes through $u$, averaged over all $v$ and $w$


| $v$ | $\mathcal{C}_{r}(v)$ |
| :---: | :---: |
| $a$ | 0.5 |
| $b$ | 0.5 |
| $c$ | 0.7 |
| $d$ | 0.4 |
| $e$ | 0.833 |

## Eigenvector-Centrality

- Value of a single vertex is determined by the values of the neighbouring vertices
- eigenvector-centrality: $\mathcal{C}_{\lambda}(u):=\sum_{v \in N(u)} \mathcal{C}_{\lambda}(v)$
- Equivalent to: $\mathcal{C}_{\lambda}\left(v_{i}\right):=\sum_{j=1}^{n} a_{i j} \mathcal{C}_{\lambda}\left(v_{j}\right)$
- Well known problem of eigenvector computation $\lambda S=A S$
- We use the eigenvector for the largest eigenvalue


| $v$ | $\mathcal{C}_{\lambda}(v)$ |
| :---: | :---: |
| $a$ | 0.497 |
| $b$ | 0.497 |
| $c$ | 0.342 |
| $d$ | 0.155 |
| $e$ | 0.604 |

## Comparing Centrality Values



| Vertex | $\mathcal{C}_{d}$ | Vertex | $\mathcal{C}_{e}$ | Vertex | $\mathcal{C}_{c}$ | Vertex | $\mathcal{C}_{r}$ | Vertex | $\mathcal{C}_{\boldsymbol{\lambda}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8 | 4 | 5 | 0.2500 | 7 | 0.0286 | 7 | 0.7429 | 7 | 0.5021 |
| 9 | 4 | 4 | 0.2000 | 6 | 0.0263 | 6 | 0.5619 | 8 | 0.4563 |
| 7 | 3 | 6 | 0.2000 | 8 | 0.0238 | 5 | 0.5143 | 9 | 0.4563 |
| 2 | 2 | 3 | 0.1667 | 9 | 0.0238 | 8 | 0.4762 | 6 | 0.2761 |
| 3 | 2 | 7 | 0.1667 | 5 | 0.0233 | 9 | 0.4762 | 10 | 0.1927 |
| 4 | 2 | 2 | 0.1429 | 4 | 0.0200 | 4 | 0.4476 | 11 | 0.1927 |
| 5 | 2 | 8 | 0.1429 | 10 | 0.0182 | 3 | 0.3619 | 12 | 0.1927 |
| 6 | 2 | 9 | 0.1429 | 11 | 0.0182 | 2 | 0.2571 | 13 | 0.1927 |
| 1 | 1 | 1 | 0.1250 | 12 | 0.0182 | 1 | 0.1333 | 14 | 0.1927 |
| 10 | 1 | 10 | 0.1250 | 13 | 0.0182 | 10 | 0.1333 | 15 | 0.1927 |
| 11 | 1 | 11 | 0.1250 | 14 | 0.0182 | 11 | 0.1333 | 5 | 0.1517 |
| 12 | 1 | 12 | 0.1250 | 15 | 0.0182 | 12 | 0.1333 | 4 | 0.0830 |
| 13 | 1 | 13 | 0.1250 | 3 | 0.0169 | 13 | 0.1333 | 3 | 0.0448 |
| 14 | 1 | 14 | 0.1250 | 2 | 0.0143 | 14 | 0.1333 | 2 | 0.0230 |
| 15 | 1 | 15 | 0.1250 | 1 | 0.0120 | 15 | 0.1333 | 1 | 0.0097 |

## Comparing Centrality Values



Centralities for the example graph


## Protein Protein Interactions for Homo sapiens

- Vertices denote proteins
- Edges denote interactions
- Undirected network
- Vertex and edge labels not shown
- Only the giant component, 563 vertices, 870 edges

Scatter plot matrix of the centrality positions for the PPI Network


## Protein Protein Interactions for Homo sapiens

Correlation coefficients for the centrality positions for the PPI-network

|  | $\mathcal{C}_{d}$ | $\mathcal{C}_{e}$ | $\mathcal{C}_{c}$ | $\mathcal{C}_{r}$ | $\mathcal{C}_{\lambda}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Degree | Eccentricity | Closeness | RWB | Eigenvector |
| $\mathcal{C}_{d}$ | - | 0.2794 | 0.3396 | 0.9534 | 0.2703 |
| $\mathcal{C}_{e}$ | 0.2794 | - | 0.4231 | 0.2776 | 0.9248 |
| $\mathcal{C}_{c}$ | 0.3396 | 0.4231 | - | 0.3843 | 0.4726 |
| $\mathcal{C}_{r}$ | 0.9534 | 0.2776 | 0.3843 | - | 0.2627 |
| $\mathcal{C}_{\lambda}$ | 0.2703 | 0.9248 | 0.4726 | 0.2627 | - |



## Centralities in Biological Networks

- Ranking of vertices according to importance
- Based on the network structure
- Many different ( $>20$ ) centrality measures exist
- None of them uses biological relevant information
- New or adapted centralities necessary


## Gene Regulatory Networks

- Genes are either transcription factors or targets genes
- Transcription factors regulate genes
- Regulatory interactions between genes form a network


Regulation of lactose degradation in E. coli Source: RegulonDB

## Global Regulators in Gene Regulatory Networks

Understanding gene regulation $\Leftrightarrow$ identification of global regulators

Different criteria for identification of global regulators:

- Number of regulated genes
- Number and type of co-regulators
- Number of other regulators they control
- Size of their evolutionary family
- Number of growth conditions under which they are active


## Centralities for Gene Regulatory Networks

- Specific centrality for the analysis of GRN necessary
- Should help in identifying global regulators
- Network motifs are relevant for GRNs!


## Motif-based Centrality

- Combination of centrality measures and network motifs
- Use the occurrences of a motif in the network
- Incorporation of functional substructures into centrality analysis


Feed-forward loop (FFL) Target graph

## Motif-based Centrality

- Combination of centrality measures and network motifs
- Use the occurrences of a motif in the network
- Incorporation of functional substructures into centrality analysis


| Vertex | Centrality |
| :---: | :---: |
| $V_{2}$ | 3 |
| $V_{3}$ | 2 |
| $V_{4}$ | 2 |
| $V_{1}$ | 1 |
| $V_{5}$ | 1 |

Feed-forward loop (FFL) Target graph
Centr. for FFL motif

## Roles of Motif Vertices

## Different vertices have different roles



Feed-forward loop


Bi-fan

## Extended Motif-based Centrality

Count the number of matches according to roles


Feed-forward loop

| Vertex | Centrality value |  |  |
| :--- | ---: | ---: | ---: |
|  | Role $A$ | Role $B$ | Role $C$ |
| $v_{2}$ | 2 | 1 | 0 |
| $v_{1}$ | 1 | 0 | 0 |
| $v_{3}$ | 0 | 1 | 1 |
| $v_{5}$ | 0 | 1 | 0 |
| $v_{4}$ | 0 | 0 | 2 |



Target graph

## Motif Classes

Motifs with similar structure grouped into motif classes

## Example: Single Input Motif (SIM)

Role A regulator for a set of genes Role B exclusively regulated genes


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Example: Single Input Motif (SIM)

Role A regulator for a set of genes Role B exclusively regulated genes


## Regulatory Chains

- One regulator regulating another, which in turn regulates a third one and so forth
- Regulators at the top of chains start regulatory cascades



## Summary: Varieties of Motif-based Centralities

Three varieties of motif-based centralities

- Plain
- With roles for the vertices of the motif
- Using classes of similar motifs

All based on the same concept:
count the matches of functional substructures in the target graph

## Gene Regulatory Network of E. coli

- Based on data from RegulonDB
- 1250 vertices and 2515 edges
- Global regulators?



## Motif-based Centrality for E. coli

| Gene | Cent. |
| :--- | ---: |
| crp | 254 |
| fnr | 203 |
| arcA | 111 |
| fis | 110 |
| narL | 100 |
| ihfAB | 61 |
| hns | 53 |
| fur | 43 |
| gadX | 34 |
| hyfR | 33 |
| marA | 29 |
| flhD | 21 |
| nagC, soxS | 19 |
| modE, tdcA, yiaJ | 18 |
| gutM, ompR, srIR | 17 |



Top 20: 10 of the 18 global regulators

Martínez-Antonio \& Collado-Vides: Identifying global regulators in transcriptional regulatory networks in bacteria, Current Opinion in Microbiology, 2003

## Extended Motif-based Centrality for E. coli

|  | Cent. |  |  |
| :--- | ---: | ---: | ---: |
| Gene | $A$ | $B$ | $C$ |
| crp | 254 | 0 | 0 |
| fnr | 150 | 53 | 0 |
| ihfAB | 61 | 0 | 0 |
| arcA | 58 | 53 | 0 |
| fis | 40 | 70 | 0 |
| modE | 18 | 0 | 0 |
| soxS | 18 | 1 | 0 |
| hns | 14 | 39 | 0 |
| fhIA | 11 | 0 | 0 |
| gadE | 11 | 0 | 0 |
| cpxR | 11 | 0 | 0 |
| rob | 10 | 0 | 0 |
| galR | 8 | 0 | 0 |
| gadX | 8 | 26 | 0 |
| gntR | 6 | 0 | 0 |
| fur | 6 | 36 | 1 |
| oxyR | 6 | 1 | 0 |
| tdcR | 6 | 0 | 0 |
| narL | 5 | 95 | 0 |
| nagC | 5 | 14 | 0 |



Top 20: 11 of the 18 global regulators

## Motif-class Centrality for E. coli

| Gene | $c_{m c c}$ | Length of chain |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  | 2 | 3 | 4 | 5 | 6 | 7 |
| crp |  | 359 | 525 | 436 | 212 | 60 | 0 |
| ihfAB |  | 186 | 215 | 156 | 82 | 28 | 0 |
| fnr |  | 206 | 237 | 27 | 0 | 0 | 0 |
| arcA |  | 111 | 215 | 127 | 17 | 0 | 0 |
| fis |  | 156 | 121 | 82 | 28 | 0 | 0 |
| evgA | 325 | 4 | 27 | 90 | 125 | 51 | 28 |
| ydeO | 322 | 1 | 27 | 90 | 125 | 51 | 28 |
| $\operatorname{gadE}$ | 321 | 27 | 90 | 125 | 51 | 28 | 0 |
| $\operatorname{soxR}$ | 213 | 2 | 24 | 92 | 91 | 4 | 0 |
| $\operatorname{soxS}$ | 211 | 24 | 92 | 91 | 4 | 0 | 0 |
| torR | 191 | 10 | 15 | 87 | 51 | 28 | 0 |
| $\operatorname{gadW}$ | 185 | 4 | 15 | 87 | 51 | 28 | 0 |
| cspE | 184 | 1 | 2 | 88 | 65 | 28 | 0 |
| cspA | 183 | 2 | 88 | 65 | 28 | 0 | 0 |
| $\operatorname{gadX}$ | 181 | 15 | 87 | 51 | 28 | 0 | 0 |
| hns | 181 | 88 | 65 | 28 | 0 | 0 | 0 |
| oxyR | 166 | 15 | 73 | 74 | 4 | 0 | 0 |
| fur | 151 | 73 | 74 | 4 | 0 | 0 | 0 |
| modE | 141 | 32 | 94 | 15 | 0 | 0 | 0 |
| narL | 109 | 94 | 15 | 0 | 0 | 0 | 0 |

# Top 20: 11 of the 18 

## Other effects:

evgA, ydeO and gadE

## Analysis of Biological Networks

(1) Motivation
(2) Foundations
(3) Network motifs
(9) Network centralities
(5) Network-related data analysis and visualisation

## Analysis in Network Context - Motivation

Integration and analysis of high-throughput data in the context of underlying processes

- Show large amounts of data in a readable and understandable form
- Consideration related networks
- Fast data evaluation (statistic tests, correlation analysis, data clustering)



## Analysis and Exploration of Data in Network Context

- Vanted features
- Creation/derivation of networks
- Data mapping onto dynamic networks
- Data analysis and visualisation methods



## Experimental Data

- Databases
- DBE
- FLAREX



## Experimental Data

- Databases
- DBE
- FLAREX
- Excel/CSV Files
- Vanted input file (metabolite, proteomics and expression data)
- J-Express files (expression data)



## Experimental Data

- Databases
- DBE
- FLAREX
- Excel/CSV Files
- Vanted input file (metabolite, proteomics and expression data)
- J-Express files (expression data)
- Programmatic
- Script API: Java/Ruby code
// @Add Experimental Datas (command will be shown in the window context menu)
int plantID = node. memGetPlantID("species", "genotype", "variety", "conditions", "treatment");
int plantID2 = node.memGetPlantID("species2", "genotype2", "variety2",
"conditions2", "treatment2");
// Time Series Data
node.memSample(5d, 1, plantID, "cm", "day", 1);
node.memSample (6d, 1, plantID, "cm", "day", 2);
node.memSample(7d, 1, plantID, "cm", "day", 3);
node.memSample(5.5d, 1, plantID2, "cm", "day", 1);
node.memSample (4.5d, 1, plantID2, "cm", "day", 2);
node.memsample (4.3a, 1, plantID2, "cm", "day", 3);
node.memAddDataMapping("C02", "g/1", " 27.2 .2006 ", "Test Experiment", "Unknown User", "Only a test", "Sequence");
int plantID = node.memGetPlantID("species", "genotype", "variety",
"conditions", "treatment");
int plantID2 = node.memGetPlantID("species2", "genotype2", "variety2", "cond1tions2", "treatment2");


## Network Data

- Databases
- MetaCrop (SBML)
- KEGG Pathway
- Reference-Pathway/

Organism-specific

- Bottom-Up
- Top-Down
- Super-Pathway



## Network Data - KEGG Specific Pathway Parts

Example: Shortest paths between the substances methane, aminosugars and ethanol


## Network Data - Exploration of KEGG Pathways



## Network Data - Exploration of KEGG Pathways



## Network Data

- Databases
- MetaCrop (SBML)
- KEGG Pathway
- Reference-Pathway/

Organism-specific

- Bottom-Up
- Top-Down
- Super-Pathway
- Ontologies / functional hierarchies
- Full GO tree
- Relevant subset
- Files
- GML, Pajek-.NET, SBML


Visualisation of gene expression time series data and corresponding gene ontology data

## Network Data

- Databases
- MetaCrop (SBML)
- KEGG Pathway
- Reference-Pathway/

Organism-specific

- Bottom-Up
- Top-Down
- Super-Pathway
- Ontologies / functional hierarchies
- Full GO tree
- Relevant subset
- Files
- GML, Pajek-.NET, SBML



## Data Integration

- Knowledge about identifiers, synonyms, associated genes and annotations
- KEGG compounds
- Expasy Enzymes
- KEGG KO
- User defined (e. g. Affymetrix)



## Data Analysis



## Data Analysis

- Visualisation methods



## Data Analysis

- Visualisation methods
- Data Charting
- Data mapping,

Ferredoxin graph-embedded view of experimental data

- Time series data (line chart)
- Non-time series data (bar charts, pie charts, ratio view)
- Filter operations (show/analyze subset, e.g. selected plant lines, selected time point(s))


26 DAF
Ferredoxin
Lhcb3
PSI-D
PIOE
Lhcbl
CPT2
CP1. 1
DiT2
TPT
ATP/ADP
XPT1


## Data Analysis

- Combination of different -omics data


Compound / Enzyme information, mapped onto a KEGG pathway

## Data Analysis

- Statistical analysis
(e.g. outliers removal, t-test)
- Correlation analysis
- Correlate time-series profile
- Correlate samples (replicate data)



## Data Analysis

- Data clustering (e.g. SOM)
- Detection of a given number of common time series patterns in the data
- Connection to external data clustering approaches


Prototype 1-> Cluster 1


Prototype 3-> Cluster 3


## Data Analysis

- Data clustering (e.g. SOM)
- Detection of a given number of common time series patterns in the data
- Connection to external data clustering approaches


Expression data map onto MapMan hierarchy

## Examples - Data Analysis (Barley)



Three phases in seed development (pre-storage, intermediate and main storage)

## Examples - Coverage of Processes (Barley)



## Examples - Data Integration (Potato)



## Examples - Data Exploration (Mouse)

Cell cycle

## down

up


## Examples - Visualisation [Tognetti et al. (2007)]



Fig. 4. Relative metabolite changes in iron-starved and control plants. Four-week-old plants were transferred to hydroponic Hoagland solution supplemented with either $\mathrm{FeSO}_{4}$-EDTA or $\mathrm{CaCO}_{3}$ ( pH 8.0 ). Leaf material was harvested after 29 days, and the corresponding metabolites were measured as described in Materia/s and Methods. Depicted are the ratios $\pm$ SE of metabolite contents between Fe-starved and-replete plants of WT (green bars), pfld5-8 (blue bars), and pfld $4-2$ (light blue bars) lines ( $n=8-10$ independent plants). The graph was created by using the visualization system Vanted (38).

## System Architecture

- Based on the extensible, plugin-based graph visualization toolkit Gravisto
- Event management (observer design pattern)
- MVC concept



## Analysis of Biological Networks

(1) Motivation
(2) Foundations
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(9) Network centralities
(6) Network-related data analysis and visualisation

## Tools

- Mavisto - motif analysis and visualisation tool
http://mavisto.ipk-gatersleben.de
- CentiBiN - centrality analysis in biological networks
http:
//centibin.ipk-gatersleben.de
- Vanted - analysis and visualisation of experimental data in the network context http://vanted.ipk-gatersleben.de
- MetaCrop - information system for plant specific metabolism http:
//metacrop.ipk-gatersleben.de
- KGML-ED - KEGG pathway explorer and editor http://kgml-ed.ipk-gatersleben.de


